4. Results

Table 1: Descriptive Statistics

	Mean	Std. Deviation	N
SL	1.4118	10.73891	240
NIFTY500	-1.0931	7.34663	240
SMB	.6927	3.79639	240
HML	.6922	4.73546	240
CMA	.1947	3.16196	240
RMW	.8774	3.44476	240
WML	1.6557	6.61594	240

Table 2: Multi-Collinearity Table

	NIFTY500	SMB	HML	CMA	RMW
SMB	.057				
HML	.136	.310			
CMA	.057	294	650		
RMW	524	293	509	.395	
WML	329	090	295	.107	.385

A quick test for multi-collinearity does not reveal any significant evidence to suggest that the independent variables are correlated to each other. The broader market proxy, in this case the NIFTY500, appears to be poorly correlated with the Size effect, and that is along expected lines. The correlation between the Market and the Value effect is twice of what is observed between the Market and the Size effect, although the correlation between the former two factors still tends to be poor. It is also observed that the correlation coefficient between the Market and the Investment effect is the same as that between the Market and the Size effect. Interestingly, the correlation coefficients between the Market and Profitability effect especially, and between the Market and Momentum effect, even though are negative, are much higher in magnitude. This becomes especially significant in light of the fact that the average returns for the Profitability effect are only second to the mean returns for the Momentum effect. These observations would be suggestive of a contrarian inclination in the behavior of these two factors in relation to the broader market movements.

Even though there is no apparent collinearity between the Size effect and the Value effect, however, the coefficient of correlation between the two is not only positive but comparatively higher. This observation seemingly suggests that usually, small-sized firms also tend to be undervalued at times. The correlation between the Size effect and the Investment effect is negative, suggesting that small-sized firms are generally not found to be conservative in their approach towards investment in assets. Similarly, the presence of a negative correlation coefficient of a similar magnitude between the Size and the Profitability effects indicate that small-sized firms also tend to have lower profitability. However, it is important to note that the correlation coefficients between neither of these factors can be considered as strong. The correlation coefficient between the Size effect and the Momentum effect is almost close to zero, alluding to the absence of any relationship between the two factors.

The coefficient of correlation observed between the Value effect and the Investment effect is also observed to be negative and on the higher side. A similar observation is recorded in the case of the Value and the Profitability effects. These observations would indicate an inclination of undervalued firms to be less conservative in their approach towards investing in assets. It would also suggest that undervalued firms tend to be less profitable in comparison to their overvalued peers. A negative correlation is also observed between the Value and Momentum effects.

The correlation coefficient found between the Investment and Profitability effect would suggest that conservative firms may tend to be among the more profitable firms as well. However, the magnitude of the correlation coefficient indicates that this conclusion might not have strong grounds for conviction. Similarly, the observed value for the Karl Pearson's correlation coefficient would suggest that conservative firms do not have a significant momentum effect.

The study observes a positive correlation between the Profitability and Momentum effect, although the magnitude of the observation does not suggest a strong correlation, it does indicate that the more profitable firms might also be found to have a significant momentum effect behind them.

CAPM

Table 3: Investment-Sorted Portfolios

Portfolio	Alpha-	Beta Coefficient	<u>t-value</u>	T-value Beta	Adjusted R
	intercept		<u>Alpha</u>		squared
P1	.00117	.795	.276	20.214	.630
P2	.00750	.814	1.86	21.652	.662
Р3	.00767	.814	1.939	21.618	.661
P4	.00689	.848	2.028	24.695	.718
P5	.00536	.845	1.652	24.386	.713
P6	.00642	.854	2.079	25.362	.729
P7	.00737	.884	2.706	29.214	.781
P8	.00582	.867	1.977	26.793	.750
P9	.00607	.898	2.189	31.415	.805
P10	.01018	.880	3.007	28.635	.774

Table 4: Market Cap-Sorted Portfolios

<u>Portfolio</u>	Alpha-	Beta Coefficient	<u>t-value</u>	<u>T-value</u>	Adjusted R
	intercept		<u>Alpha</u>		squared
P1	.01688	.721	3.120	16.036	.517
P2	.00936	.763	1.984	18.186	.580
Р3	.00708	.801	1.666	20.623	.640
P4	.00650	.817	1.642	21.835	.666
P5	.00632	.836	1.716	23.481	.697
P6	.00353	.857	1.053	25.689	.734
P7	.00420	.885	1.427	29.378	.783
P8	.00293	.895	1.065	30.883	.799
P9	00073	.927	350	38.018	.858
P10	.00021	.971	.177	62.366	.942

Table 5: Profitability-Sorted Portfolios

<u>Portfolio</u>	Alpha-	<u>Beta</u>	<u>T-value</u>	<u>T-value</u>	Adjusted R
	<u>intercept</u>	<u>Coefficient</u>	<u>Aplha</u>		<u>squared</u>
P1	.00287	.829	.666	22.849	.686
P2	.00585	.822	1.418	22.286	.675
P3	.00716	.855	1.894**	25.476	.731
P4	.00454	.831	1.217	23.054	.689
P5	.00591	.845	1.704**	24.415	.713
P6	.00547	.825	1.547	22.505	.679
P7	.00663	.870	2.354*	27.253	.756
P8	.00689	.881	2.608*	28.723	.775
P9	.00914	.893	3.738*	30.575	.796
P10	.00990	.885	3.710*	29.391	.783

Table 6: Value-Sorted Portfolios

Portfolio	Alpha-	Beta Coefficient	T-value	T-value	Adjusted R
	<u>intercept</u>		<u>Aplha</u>		<u>squared</u>
P1	.01349	.735	2.450	16.746	.539
P2	.00954	.783	2.119	19.397	.611
Р3	.00866	.814	2.154	21.629	.661
P4	.00789	.816	2.042	21.817	.665
P5	.00608	.856	1.847	25.588	.732
P6	.00721	.864	2.223	26.496	.746
P7	.00210	.888	.748	29.863	.788
P8	.00179	.892	.659	30.523	.796
P9	.00005	.907	.019	33.266	.822
P10	00081	.928	402	38.531	.861

Table 7: Momentum-Sorted Portfolios

Portfolio	Alpha-	Beta Coefficient	<u>T-Value</u>	<u>T-value</u>	Adjusted R
	<u>intercept</u>		<u>Alpha</u>		<u>squared</u>
P1	00339	.758	611	17.944	.573
P2	.00158	.716	.338	15.843	.511
Р3	.00529	.728	1.299	16.383	.528
P4	.00693	.738	1.732	16.855	.542
P5	.00873	.740	2.226	16.995	.546
P6	.00983	.727	2.559	16.356	.527
P7	.00971	.708	2.449	15.469	.499
P8	.01120	.714	2.921	15.728	.508
P9	.01265	.676	3.033	14.170	.455
P10	.01494	.598	2.922	11.511	.355

Tables 3 to 7 present regression results of the single-factor CAPM. The returns of single-sorted portfolios have been regressed against the mean-excess broader market returns, and some of the results are very interesting. Even though the CAPM is able to adequately explain the average returns on all but one of the ten portfolios formed on the basis of market capitalization, it fails to perform sufficiently when applied to portfolios formed on factors other than market cap. This interpretation is supported by the argument that a model that has significant explanatory powers will have an Alpha-intercept that will be very close to zero. The results show that the CAPM especially falls short in explaining average returns on portfolios P1 sorted on Investment, P1 sorted on Market Cap and P1 sorted on the Value factor as well. It is important to note that there are other portfolios sorted on the basis of the aforementioned factors

that have statistically significant Alpha-values as well, however, I have chosen to highlight results for portfolios that have an Alpha-intercept greater than .009. The results reveal a great deal about how the investors perceive stocks of certain companies. The results provide testimony to the presence of size and value factor, with the portfolio of the smallest-size companies by way of market cap generally being companies that also tend to have the highest value as measured by the PB ratio. Additionally, the results also present a strong argument against the strength of the CAPM in explaining returns of companies that are aggressively reinvesting their earnings to acquire new assets, as evidenced by the significant outperformance of the portfolio P10 formed on the Investment factor. It has commonly been observed that small-size, high value companies also tend to invest aggressively in assets, thus one may infer that a majority of the companies comprising the single-sorted portfolios P1 formed on market cap, P1 formed on the basis of value factor and P10 formed on the basis of the Investment factor might overlap. However, the most interesting results were observed when single-sorted portfolios formed on the basis of the Momentum factor were regressed against the market returns. Three portfolios, namely P8, P9 and P10, the ones that had the strongest momentum effects in their favor, also had statistically significant Alpha values of greater than .009, implying that the single-factor CAPM was especially inept at explaining momentum returns. The values of the adjusted R squared are also indicative of the aforementioned inability of the single-factor Capital Asset Pricing-model. These results stand to confirm previous literature

Fama-French Three-Factor model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_t + \varepsilon_{it}$$

which has found the CAPM inadequate in explaining excess portfolio returns.

Table 8: Investment-sorted Portfolios

<u>Portfolio</u>	Alpha	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-</u>	T-value2	<u>T-value3</u>	Adjusted R ²
					<u>valueA</u>	<u>value1</u>			
P1	00975	.749	.387	.172	-3.520	29.490	14.596	6.462	.849
P2	00339	.766	.355	.208	-1.345	33.116	14.729	8.572	.875
Р3	00338	.763	.358	.227	-1.458	35.037	15.800	9.916	.889
P4	00112	.813	.324	.119	457	33.248	12.722	4.626	.860
P5	00250	.803	.272	.197	-1.065	32.471	10.556	7.589	.857
P6	00670	.820	.293	.132	288	32.905	11.305	5.043	.854
P7	.00101	.851	.254	.137	.500	38.306	10.973	5.856	.884
P8	00053	.834	.250	.136	229	33.011	9.509	5.129	.850
P9	.00081	.878	.254	.037	.356	38.111	10.575	1.547	.876
P10	.00560	.876	.301	093	2.016*	35.211	11.599	-3.564	.855

Table 9: Market Cap-Sorted Portfolios

Portfolio	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-</u>	T-value2	T-value3	Adjusted R ²
					<u>ValueA</u>	<u>value1</u>			
P1	.00063	.664	.554	.183	.277	35.504	28.402	9.298	.918
P2	00426	.713	.502	.157	-1.838	35.154	23.766	7.398	.904
Р3	00510	.753	.442	.167	-2.310	37.858	21.347	8.008	.907
P4	00403	.775	.409	.134	-1.683	34.748	17.611	5.703	.883
P5	00261	.799	.346	.127	-1.011	32.465	13.477	4.903	.858
P6	00385	.823	.260	.147	-1.466	31.951	9.690	5.429	.845
P7	00078	.861	.177	.106	297	32.500	6.416	3.812	.835
P8	00102	.874	.141	.090	398	32.845	5.101	3.217	.834
P9	00270	.915	.070	.059	-1.314	38.533	2.843	2.383	.868
P10	.00003	.969	.002	.013	.025	61.499	.092	.759	.942

Table 10: Profitability-Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	T-value1	T-value2	T-value3	Adjusted R ²
					<u>ValueA</u>				
P1	00858	.785	.359	.172	-3.149	34.747	15.248	7.260	.880
P2	00466	.778	.337	.184	-1.670	31.606	13.120	7.118	.858
P3	00230	.820	.338	.121	903	36.770	14.556	5.184	.883
P4	00509	.788	.335	.180	-2.055	33.354	13.619	7.256	.869
P5	00248	.807	.308	.154	995	32.965	12.088	5.975	.859
P6	00276	.785	.305	.167	-1.044	29.078	10.861	5.875	.829
P7	.00003	.834	.261	.155	.013	35.629	10.686	6.290	.871
P8	.00114	.852	.265	.100	.555	36.281	10.834	4.072	.871
P9	.00442	.872	.263	.040	2.230	37.381	10.810	1.629	.872
P10	.00625	.878	.274	064	2.751	34.762	10.393	-2.418	.850

Table 11: Value-Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
					<u>Value</u>	value1	value2	value3	<u>R</u> ²
P1	00339	.673	.486	.258	-	35.750	24.793	13.080	.917
					1.416				
P2	00377	.724	.398	.267	-	35.597	18.770	12.499	.903
					1.638				
Р3	00297	.762	.384	.220	-	38.240	18.461	10.506	.907
					1.374				
P4	00240	.771	.367	.183	983	33.094	15.124	7.480	.873
P5	00177	.820	.298	.142	741	34.261	11.952	5.639	.866
P6	00006	.832	.287	.114	026	34.048	11.282	4.428	.860
P7	00330	.863	.219	.095	-	34.943	8.508	3.682	.857
					1.395				
P8	00222	.881	.243	016	939	34.977	9.250	617	.851
P9	00238	.902	.176	037	-	35.596	6.658	-1.358	.849
					1.037				
P10	00178	.935	.160	113	965	42.703	7.036	-4.921	.888

Table 12: Momentum-Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-</u>	T-value2	T-value3	Adjusted
					<u>ValueA</u>	<u>value1</u>			<u>R</u> ²
P1	01398	.724	.320	.122	-2.988	20.619	8.741	3.300	.711
P2	00808	.666	.263	.264	-2.112	18.274	6.923	6.912	.689
Р3	00356	.675	.266	.281	-1.106	19.503	7.368	7.722	.719
P4	00133	.690	.275	.233	407	19.550	7.465	6.274	.708
P5	.00068	.695	.282	.218	.211	19.688	7.679	5.882	.708
P6	.00227	.682	.271	.220	.703	18.521	7.064	5.675	.682
P7	.00200	.663	.285	.213	.596	17.393	7.178	5.319	.659
P8	.00469	.681	.301	.119	1.389	17.160	7.290	2.860	.631
P9	.00659	.647	.282	.096	1.712	14.895	6.236	2.112	.557
P10	.01054	.589	.281	051	2.128	11.874	5.435	988	.423

In contrast, when regressing the returns of the same single-sorted portfolios against the Fama-French Three-Factor model, it is found that some portfolios that were previously found to have statistically significant outperformance when tested in the CAPM are unable to display the same when their returns are regressed against the Fama-French three factors. In other instances where portfolios that still manage to outperform the Three-factor model, the values of the Alpha-intercept are lower than those observed for the same portfolios when regressed against the single-factor model. For a single-sorted portfolios based on the Investment factor, the portfolio P10, comprising of companies that are most aggressively investing in assets, has a

statistically significant Alpha-intercept. This implies that the portfolio has managed to outperform the model. However, the outperformance, as measured by the Alpha-intercept, pales when compared with that of the same portfolio when tested against the CAPM, suggesting that the Fama-French Three-factor model at least does a better job than the CAPM in explaining excess portfolio returns. Similarly, portfolios P9 and P10, comprising of the most profitable listed firms, still manage to outperform the Three-factor model, as evident by the statistically significant Alpha-intercept. However, the Alpha generated by these portfolios is lesser than that generated by the same portfolios when regressed against the CAPM. The tests show that FF Three-Factor model does a great job in explaining excess returns for portfolios formed on the basis of size and value. Yet, for portfolios formed on the momentum factor, it is found that the portfolio P10, having the strongest momentum effect, still manages to retain its statistically significant Alpha from before.

Carhart Four-factor model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_{it} + \beta_3 MOM_{it} + \varepsilon_{it}$$

Table 13: Investment-Sorted Portfolio

Portfolio	<u>Alpha</u>	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>ValueA</u>	value1	value2	value3	value4	<u>R</u> ²
7.1	00.50	5 0.5	200	105	1.10	2 20 5	20.155	17.770	7.102	5 (5 0)	0.55
P1	0059	.706	.388	.135	148	-2.206	28.155	15.570	5.183	-5.679	.866
P2	0003	.731	.356	.178	119	129	31.560	15.475	7.412	-4.944	.886
Р3	0008	.733	.359	.201	100	374	33.288	16.420	8.819	-4.359	.897
P4	.00167	.779	.325	.089	117	.685	31.580	13.280	3.476	-4.583	.871
P5	.00030	.766	.273	.165	124	.128	30.879	11.074	6.430	-4.825	.869
P6	.00225	.781	.294	.098	132	.991	31.413	11.931	3.807	-5.135	.869
P7	.00273	.828	.255	.116	079	1.333	36.242	11.230	4.917	-3.352	.889
P8	.00239	.795	.251	.102	134	1.045	31.511	10.036	3.897	-5.111	.865
P9	.00358	.843	.255	.007	118	1.601	36.551	11.122	.292	-4.954	.887
P10	.00909	.837	.301	127	131	3.329	33.711	12.231	-4.935	-5.101	.869

Table 14: Market Cap-Sorted Portfolio

<u>Portfolio</u>	Alpha	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>Value</u>	value1	value2	value3	value4	$\underline{\mathbf{R}^2}$
P1	.00263	.644	.554	.165	069	1.138	33.533	29.074	8.301	-3.454	.922
P2	0016	.684	.503	.133	096	725	33.446	24.747	6.276	-4.503	.911
P3	0026	.725	.443	.143	095	-	36.151	22.259	6.881	-4.575	.914
						1.185					
P4	0009	.740	.410	.103	120	414	33.290	18.597	4.466	-5.215	.895
P5	.00079	.759	.346	.092	136	.311	31.057	14.289	3.625	-5.383	.873
P6	0006	.784	.261	.113	130	266	30.376	10.179	4.239	-4.875	.858
P7	.00324	.811	.178	.062	171	1.292	31.522	6.982	2.334	-6.411	.859
P8	00200	.823	.143	.045	175	1.225	31.957	5.581	1 602	-6.573	950
Po	.00299	.823	.143	.043	173	1.223	31.937	3.381	1.683	-0.373	.859
P9	.00014	.874	.071	.024	138	.071	37.330	3.064	.984	-5.7	.883
P10	.00159	.944	.002	009	084	1.318	60.099	.131	557	-5.166	.947
FIU	.00139	.744	.002	009	004	1.510	00.033	.131	1551	-5.100	.74/

Table 15: Profitability-sorted portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>Value</u>	value1	value2	value3	value4	<u>R</u> ²
P1	0053	.751	.360	.143	114	-	33.154	15.99	6.094	-4.846	.891
						1.979					
P2	0005	.733	.338	.145	152	209	30.471	14.134	5.816	-6.111	.877
Р3	.0005	.789	.339	.095	103	.197	35.019	15.145	4.065	-4.418	.892
7.1	0010	550	22.5	4.45	105	505	21.000	11.20.5	5.050	7.20.5	002
P4	0019	.750	.336	.147	127	795	31.888	14.386	6.050	-5.206	.882
P5	.00071	.768	.309	.120	132	.292	31.504	12.778	4.742	-5.224	.874
P6	.00105	.737	.307	.124	164	.414	27.840	11.674	4.541	-5.983	.851
P7	.00226	.803	.261	.128	105	1.083	33.849	11.099	5.196	-4.279	.880
P8	.00350	.819	.266	.071	114	1.724	34.613	11.328	2.906	-4.651	.881
P9	.00646	.843	.264	.014	101	3.263	35.530	11.197	.565	-4.125	.880
P10	.00856	.847	.274	092	108	3.766	32.937	10.756	-3.458	-4.063	.859

Table 16: Value-Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>ValueA</u>	<u>value1</u>	<u>value2</u>	<u>value3</u>	<u>value4</u>	<u>R</u> ²
P1	0012	.652	.487	.240	072	510	33.796	25.428	12.030	-3.577	.921
P2	0008	.692	.398	.239	109	374	34.131	19.806	11.388	-5.185	.913
P3	0004	.733	.384	.195	098	204	36.592	19.312	9.384	-4.738	.915
P4	.00152	.724	.368	.142	158	.659	32.325	16.549	6.141	-6.787	.893
P5	.0011	.784	.299	.110	124	.499	32.725	12.579	4.431	-5.006	.878
P6	.00349	.789	.288	.075	149	1.471	32.911	12.124	3.043	-5.986	.878
P7	0000	.821	.220	.058	144	010	33.694	9.097	2.319	-5.709	.874
P8	.00184	.827	.244	063	182	.834	34.625	10.286	-2.553	-7.356	.879
P9	.00090	.857	.177	076	153	.407	34.460	7.162	-2.957	-5.926	.868
P10	0011	.925	.161	122	033	590	40.325	7.059	-5.120	-1.383	.888

Table 17: Momentum-Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>Adjusted</u>
						<u>Value</u>	<u>value1</u>	<u>value2</u>	<u>value3</u>	<u>value4</u>	<u>R</u> ²
P1	0028	.620	.322	.031	353	726	21.011	10.996	1.011	-11.547	.815
P2	0041	.619	.264	.224	157	-1.088	16.726	7.177	5.845	-4.092	.708
Р3	0026	.663	.266	.270	040	805	18.254	7.377	7.190	-1.064	.719
P4	0010	.686	.275	.229	014	302	18.473	7.454	5.958	365	.706
P5	0015	.725	.282	.245	.104	478	19.843	7.766	6.467	2.741	.716
P6	0008	.726	.270	.257	.148	246	19.281	7.235	6.610	3.781	.699
P7	0024	.726	.284	.268	.214	753	19.207	7.567	6.847	5.454	.696
P8	0022	.781	.299	.207	.342	744	21.860	8.433	5.599	9.241	.728
P9	0020	.768	.280	.202	.412	632	20.406	7.487	5.190	10.556	.698
P10	0029	.756	.277	.094	.568	779	19.868	7.344	2.398	14.393	.692

Interesting results are observed when regressing the mean excess returns of single-sorted portfolios against the Carhart Four-Factor model. The aforementioned model is essentially a Fama-French Three-Factor model that has a Momentum factor added to it. Unlike previous observations, single-sort portfolios formed on the basis of the momentum effect fail to show a statistically significant value for the Alpha-intercept. This would suggest that the addition of a Momentum factor to the three already included in the Fama-French model helps to account for the outperformance of momentum portfolios observed previously. Similarly, portfolios formed on the basis of the Size and the Value effect also fail to outperform the model. However, it is

still important to note that for single-sorted portfolios formed on the basis of the investment factor, the portfolio P10, consisting of companies that have been the most aggressive in enlarging their asset size, the model still fails to explain the outperformance of the particular portfolio. Likewise, for single-sorted portfolios P9 and P10, formed on the basis of the profitability factor, the Alpha-intercept is still statistically significant; thereby implying that the Four-Factor model is unable to explain the excess returns for portfolios comprising of the most profitable companies and for portfolios consisting of companies that have displayed the most aggressive approach towards asset acquisition. However, the values of the adjusted R squared indicate that both the Fama-French Three-Factor model and the Carhart Four-Factor model do a far better job than the CAPM in explaining mean excess returns for portfolios.

Fama-French 5 Factor Model

 $R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_t + \beta_4 CMA_t + \beta_5 RMW_t + \varepsilon_{it}$

Table 18: Investment-Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	Adj. R ²
P1	0023	.710	.350	.013	163	13	88	25.122	14.377	.406	-5.194	-4.25	.877
P2	.00174	.735	.330	.100	106	10	.677	27.158	14.142	3.250	-3.524	-3.264	.888
Р3	.00064	.731	.338	.145	070	09	.267	28.151	15.122	4.913	-2.441	-3.084	.897
P4	.00095	.752	.313	.106	.053	11	.368	25.393	12.294	3.144	1.608	-3.431	.866
P5	0007	.802	.262	.146	065	02	29	26.385	10.009	4.243	-1.920	660	.858
P6	.00050	.796	.287	.114	.003	05	.199	25.847	10.811	3.258	.094	-1.405	.854
P7	.00105	.827	.254	.153	.050	03	.479	30.164	10.765	4.925	1.630	-1.185	.885
P8	0003	.790	.249	.160	.081	06	12	25.602	9.374	4.575	2.363	-1.916	.854
P9	0011	.838	.265	.120	.154	03	48	30.860	11.321	3.900	5.088	-1.197	.887
P10	.00482	.786	.305	01	.210	12	1.78	28.146	12.672	302	6.780	-3.929	.880

Table 19: Market Cap-Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
P1	.00502	.625	.534	.112	05	10	2.129	28.242	28.064	4.442	-	-	.925
											1.936	3.994	

P2	.00106	.649	.477	.074	04	15	.457	27.824	23.754	2.798	-	-	.917
											1.400	5.597	
P3	0024	.722	.429	.123	02	07	-	29.809	20.592	4.466	849	-	.910
							1.039					2.669	
P4	0034	.730	.407	.151	.074	07	-	26.870	17.392	4.894	2.464	-	.887
							1.351					2.399	
P5	0003	.758	.334	.095	.004	09	110	25.152	12.858	2.768	.130	-	.861
												2.493	
P6	0010	.777	.245	.104	00	.101	367	24.725	9.066	2.903	123	-	.849
												2.789	
P7	.00092	.794	.168	.106	.076	12	.333	24.789	6.091	2.913	2.122	-	.843
												3.257	
P8	.00146	.802	.128	.070	.057	13	.541	25.010	4.630	1.934	1.595	-	.842
												3.765	
P9	0014	.883	.063	.043	.016	06	671	30.172	2.495	1.306	.477	-	.869
												1.917	
P10	.00025	.963	.000	.009	.001	01	.188	49.254	.000	.396	.068	522	.941

Table 20: Profitability-Sorted Portfolios

Portfolio	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
P1	0005	.677	.323	.064	02	24	198	28.050	15.556	2.348	650	-8.69	.911

P2	.00115	.696	.309	.101	01	18	.409	24.367	12.575	3.114	457	-	.875
												5.603	
Р3	.00339	.694	.312	.073	.080	24	1.427	29.154	15.205	2.717	3.038	-	.913
												9.024	
P4	0013	.741	.316	.113	03	11	493	26.087	12.905	3.497	-	-	.876
											1.092	3.447	
P5	.00015	.752	.295	.121	.021	11	.055	25.304	11.512	3.599	.621	-	.865
												3.293	
P6	0007	.750	.295	.135	00	08	269	22.575	10.297	3.577	043	-	.831
												1.989	
P7	0005	.828	.264	.176	.034	00	228	28.554	10.571	5.333	1.058	051	.871
P8	0008	.886	.277	.139	.011	.078	388	30.795	11.192	4.253	.356	2.360	.873
P9	.00153	.912	.281	.106	.042	.099	.732	32.344	11.587	3.315	1.331	3.047	.878
P10	.00336	.920	.291	00	.031	.099	1.392	29.942	11.004	128	.911	2.816	.855

Table 21: Value-Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²

P1	.00169	.617	.465	.188	03	-	.693	28.176	24.645	7.550	-1.19	-	.926
						.13						5.17	
						.13						3.17	
P2	0011	.684	.385	.230	00	-	46	27.659	18.087	8.206	083	-	.906
						.09						3.06	
P3	0022	.743	.380	.213	.013	-	93	30.125	17.872	7.613	.480	-	.907
						.04						1.32	
P4	.00096	.710	.350	.138	.010	-	.375	25.388	14.532	4.336	.325	-	.880
						.13						4.00	
P5	.00071	.784	.285	.099	01	-	.278	26.769	11.295	2.973	453	-	.868
						.08						2.48	
P6	.00112	.799	.281	.105	.026	-	.421	26.523	10.834	3.061	.771	-	.861
						.06						1.82	
P7	0018	.821	.211	.083	.031	-	72	27.089	8.077	2.414	.924	-	.859
						.08						2.30	
P8	0000	.812	.231	03	.060	-	03	26.771	8.833	877	1.787	-	.859
						.13						3.73	
P9	.00024	.851	.160	08	.002	-	.098	27.609	6.045	-2.28	.066	-	.854
						.11						3.13	
P10	.00044	.882	.146	15	.014	-	.225	33.344	6.430	-4.93	.479	-	.893
						.11						3.61	

Table 22: Momentum-Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>B1</u>	<u>B2</u>	<u>B3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													$\underline{\mathbf{R}^2}$

P1	0049	.576	.284	.040	.061	-	-1.063	14.373	8.213	.871	1.358	-6.51	.753
						.30							
P2	0029	.542	.237	.217	.079	_	738	12.584	6.387	4.442	1.660	-4.93	.716
12	.002)	.542	.231	.217	.075	.24	.730	12.504	0.507	7,772	1.000	4.73	.710
						.21							
P3	0010	.610	.251	.253	.037	-	308	14.404	6.894	5.252	.792	-2.64	.725
						.12							
P4	.00265	.607	.252	.173	.017	_	.766	14.224	6.848	3.573	.358	-3.56	.720
1 4	.00203	.007	.232	.175	.017	.17	.700	14.224	0.040	3.373	.556	-3.50	.720
						•17							
P5	.00525	.616	.256	.136	01	-	1.548	14.487	6.979	2.810	378	-3.61	.723
						.17							
P6	.00470	.613	.256	.192	.043	_	1.361	13.601	6.606	3.756	.857	-2.62	.688
FO	.00470	.013	.230	.172	.043	.13	1.301	13.001	0.000	3.730	.037	-2.02	.000
						.13							
P7	.00457	.631	.269	.154	04	-	1.268	13.436	6.658	2.893	771	-1.51	.662
						.08							
P8	.00797	.632	.281	.047	03	_	2.204	12.989	6.699	.857	706	-2.11	.637
10	.00797	.032	.201	.047	03	.11	2.204	12.909	0.099	.037	700	-2.11	.037
						.11							
P9	.00955	.610	.264	.030	04	-	2.304	11.392	5.734	.500	737	-1.53	.560
						.09							
P10	.01353	.559	.265	11	04	_	2.531	9.109	5.015	-1.61	662	-1.14	.423
F 10	.01555	.339	.203	11	04	.08	2.331	9.109	3.013	-1.01	002	-1.14	.423
						.00							
L	L	ı			·	l	·			·	1	L	

When the single-sorted portfolios are regressed against the Fama-French Five-Factor model, it is found that except for portfolios sorted on the momentum effect, the model is sufficiently able to explain the mean excess returns. The only exceptions to the aforementioned observations is a portfolio of the smallest companies by way of market cap, P1, which has statistically significant outperformance as measured by the Alpha-intercept; and the portfolio P10, which comprises of companies which have shown the most aggressive asset growth, although the Alpha-intercept is only statistically significant when using the 10 % confidence interval.

However, on the whole, the observed values of the adjusted R squared strongly suggest that the FF five-factor model can be considered as robust in explaining excess portfolio returns. However, the same conclusion cannot be drawn for the model when testing it against portfolios sorted using the momentum effect. For single-sorted momentum portfolios P8, P9 and P10, the Alpha-intercept is not only statistically significant but its value, especially for the momentum portfolio P10, is similar to the ones observed for the same portfolios when tested against the CAPM and the Fama-French Three-Factor model. Therefore, it would suffice to say that the Fama-French Five-Factor model fails to explain the excess returns of portfolios formed on the basis of the momentum effect.

Modified Five-Factor Model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 CMA_t + \beta_4 RMW_t + \beta_5 MOM_{it} + \varepsilon_{it}$$

Table 23: Investment-Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	Adj.
													<u>R</u> ²
P1	.00017	.686	.352	17	-	-	.072	25.799	15.632	-6.86	-3.35	-6.08	.894
					.10	.14							
P2	.00623	.715	.338	16	-	-	2.611	27.145	15.159	-6.44	-3.09	-5.51	.896
					.09	.13							
Р3	.00595	.714	.350	15	-	-	2.552	27.200	15.744	-5.97	-3.32	-4.95	.897
					.10	.11							
P4	.00508	.734	.322	00	-	-	2.072	25.024	12.981	071	-3.38	-4.53	871
					.11	.11							
P5	.00446	.779	.274	14	-	-	1.886	26.006	10.804	-5.05	588	-5.60	.866
					.02	.14							
P6	.00486	.773	.296	05	-	-	2.091	25.778	11.667	-2.00	-1.15	-5.47	865
					.04	.14							
P7	.00553	.813	.266	03	-	-	2.572	28.789	11.140	-1.15	-1.60	-3.86	.881
					.05	.09							
P8	.00503	.768	.262	00	-	-	2.130	24.994	10.083	078	-1.99	-5.41	858
					.06	.14							
P9	.00338	.819	.275	.091	-	-	1.537	30.568	12.114	3.661	-1.11	-5.31	893
					.03	.12							
P10	.00625	.768	.305	.216	-	-	2.471	28.263	13.245	8.543	-3.04	-4.38	889
					.09	.10							

Table 24: Market Cap-Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
P1	.00949	.614	.543	10	11	07	4.126	27.147	28.393	-5.03	-4.32	-3.82	.923
P2	.00450	.635	.483	07	14	09	2.053	27.574	24.797	-3.49	-5.55	-4.49	.921
Р3	.00240	.706	.440	09	08	10	1.066	29.085	21.386	-3.84	-2.80	-4.98	.912
P4	.00230	.710	.419	00	07	12	.949	26.143	18.223	160	-2.55	-5.48	.890
P5	.00410	.736	.342	04	07	13	1.609	25.220	13.842	-1.65	-2.17	-5.49	.872
P6	.00335	.755	.254	06	09	13	1.283	24.561	9.755	-2.03	-2.59	-4.99	.858
P7	.00575	.767	.177	.021	10	17	2.284	25.152	6.865	.730	-2.90	-6.33	.861
P8	.00534	.774	.134	.021	11	17	2.198	25.612	5.246	.730	-3.21	-6.30	.863
P9	.00108	.860	.067	01	04	14	.539	30.824	2.839	262	-1.16	-5.60	.883
P10	.00136	.949	.001	00	.010	08	1.110	50.569	.077	166	.498	-5.14	.947

<u>Table 25: Profitability-Sorted Portfolios</u>

<u>Portfolio</u>	<u>α</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	Adj.
													<u>R²</u>
P1	.00293	.661	.329	05	23	-	1.236	27.970	16.415	-2.30	-8.68	-	.916
						.09						4.60	
P2	.00617	.672	.318	07	17	-	2.390	24.553	13.71	-2.63	-5.48	-	.888
						.14						6.10	
Р3	.00664	.681	.318	.042	24	-	2.942	28.737	15.826	1.917	-9.13	-	.916
						.08						3.86	
P4	.00344	.720	.325	09	10	-	1.417	25.930	13.825	-3.60	-3.35	-	.884
						.13						5.44	
P5	.00498	.731	.305	04	11	-	2.014	25.048	12.337	-1.57	-3.22	-	.872
						.13						5.32	
P6	.00475	.722	.306	07	06	-	1.825	22.616	11.320	-2.41	-1.70	-	.847
						.17						6.28	
P7	.00478	.809	.278	06	01	-	2.171	27.403	11.133	-2.09	341	-	.869
						.13						5.03	
P8	.00376	.864	.289	06	.082	-	1.829	30.597	12.085	-2.31	2.601	-	.881
						.14						5.84	
P9	.00516	.891	.290	01	.107	-	2.648	32.332	12.428	521	3.460	-	.886
						.13						5.29	
P10	.00480	.899	.291	.034	.135	-	2.152	30.185	11.557	1.218	4.041	-	.867
						.12						4.56	

Table 26: Value-Sorted Portfolios

<u>Portfolio</u>	<u>α</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R²</u>
P1	.00875	.606	.480	13	-	08	3.459	25.378	23.727	-5.70	-	-	.915
					.16						5.82	4.07	
P2	.00706	.665	.404	12	-	13	2.814	25.017	17.925	-4.94	-	-	.894
					.11						3.69	5.72	
Р3	.00511	.725	.397	10	-	12	2.156	27.628	17.844	-4.00	-	-	.897
					.06						1.99	5.45	
P4	.00673	.684	.362	06	-	16	2.880	25.551	15.940	-2.46	-	-	.893
					.12						3.94	6.99	
P5	.00485	.763	.293	07	-	13	2.041	26.709	12.118	-2.48	-	-	.878
					.07						2.24	5.20	
P6	.00581	.774	.290	03	-	15	2.400	26.854	11.886	-1.06	-	-	.875
					.05						1.42	6.18	
P7	.002	.798	.218	01	-	14	.861	27.424	8.860	438	-	-	.873
					.06						1.84	5.72	
P8	.00143	.784	.229	.076	-	16	.642	27.661	9.562	2.901	-	-	.880
					.07						2.37	6.43	
P9	.00023	.827	.155	.044	-	13	.101	27.531	6.097	1.589	-	-	.865
					.05						1.54	4.87	
P10	0025	.880	.135	.091	-	.003	-1.257	31.289	5.673	3.497	-	.129	.882
					.07						2.25		

Table 27: Momentum-Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	Adj.
													<u>R</u> ²
P1	.00240	.521	.289	.041	-	32	.658	15.881	10.385	1.332	-	-11.16	.839
					.22						5.90		
P2	.00470	.519	.254	03	-	15	1.225	11.837	6.855	821	-	-4.068	.712
					.26						5.22		
P3	.00516	.604	.271	09	-	06	1.478	13.410	7.104	-2.25	-	-1.520	.696
					.18						3.55		
P4	.00659	.608	.265	07	-	02	1.923	13.705	7.063	-1.78	-	449	.705
					.22						4.34		
P5	.00673	.637	.265	09	-	.104	2.055	14.804	7.280	-2.22	-	2.790	.722
					.24						5.04		
P6	.00684	.641	.270	06	-	.138	2.045	13.995	6.968	-1.35	-	3.458	.686
					.23						4.44		
P7	.00518	.669	.280	12	-	.198	1.537	14.542	7.184	-2.84	-	.198	.683
					.18						.182		
P8	.00462	.694	.282	06	-	.347	1.559	16.596	7.966	-1.64	-	9.557	.738
					.23						4.96		
P9	.00484	.684	.264	06	-	.416	1.480	15.449	7.045	-1.48	-	10.817	.706
					.22						4.53		
P10	.00240	.660	.252	.012	-	.591	.660	15.077	6.807	.297	-	15.525	.713
					.22						4.55		

According to Fama-French (2015), including the Profitability factor in the pricing model renders the Value factor as obsolete. Therefore, as an experiment, the Value factor is removed. At the same time, the Momentum factor is added to the model. Thus, even though portfolio returns are still regressed against a model containing five factors, however, the factors are not all the same as the ones in the Fama-French Five-Factor model. What is observed is extremely

fascinating. It is found that for single-sorted portfolios formed on the basis of the Investment factor, almost all the portfolios show a statistically significant Alpha-intercept. Similarly, most of the portfolios formed using the Profitability factor also outperform the model at a statistically significant level. Moreover, portfolios P1 & P2, formed on the basis of market capitalization and which consist of the smallest listed companies, also outperform the model at a statistically significant level. Additionally, it is found that single-sort value portfolios consisting of high value companies, and even those comprising of those companies that have been classified as being neutral from a value perspective, show a statistically significant Alpha-intercept. However, the model is able to explain most of the excess returns for momentum portfolios.

Six-Factor model

$$\begin{split} R_{pt} - R_{ft} &= \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_t + \beta_4 CMA_t + \beta_5 RMW_t + \\ \beta_6 MOM_{it} + \varepsilon_{it} \end{split}$$

Table 28: Investment-Sorted Portfolios

<u>P</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj.
															<u>R</u> ²
P1	.00079	.686	.354	02	18	10	14	.308	25.767	15.60	734	-6.17	-3.43	-6.10	.894
P2	.00427	.715	.332	.072	12	07	11	1.709	27.437	14.97	2.399	-4.18	-2.50	-5.01	.898
P3	.00269	.715	.340	.121	08	07	09	1.127	28.176	15.766	4.189	-2.94	-2.40	-4.23	.904
P4	.00305	.734	.316	.080	.040	09	10	1.188	25.299	12.792	2.418	1.245	-2.78	-4.04	.874
P5	.00172	.780	.265	.115	08	.006	13	.703	26.620	10.631	3.426	-2.50	.186	-4.98	.871
P6	.00294	.774	.290	.082	01	02	13	1.208	26.059	11.470	2.412	401	585	-4.96	.868
P7	.00242	.814	.256	.135	.040	02	07	1.106	29.894	11.040	4.333	1.338	646	-3.10	.889
P8	.00202	.769	.252	.130	.065	04	12	.831	25.727	9.915	3.791	1.980	-1.14	-4.74	.866
P9	.00106	.819	.267	.093	.140	01	11	.466	31.148	11.944	3.101	4.812	407	-4.72	.896
P10	.00727	.768	.308	04	.197	10	10	2.720	28.276	13.306	-1.17	6.565	-3.24	-4.53	.890

Table 29: Market Cap-Sorted Portfolios

<u>P</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj. R ²
P1	.00650	.614	.536	.097	05	-	-	2.756	27.964	28.658	3.848	-2.27	-	-3.127	.928
						.08	.06						3.460		
P2	.00294	.635	.479	.054	05	-	-	1.279	27.780	24.618	2.067	-1.84	-	-4.042	.922
						.13	.08						4.984		
Р3	0004	.707	.432	.101	03	-	-	183	29.903	21.458	3.726	-1.31	-1.97	-4.313	.916
						.05	.09								
P4	0010	.711	.409	.124	.060	-	-	418	27.048	18.302	4.116	2.082	-	-4.772	.897
						.05	.11						1.637		
P5	.00244	.736	.337	.063	01	-	1	.910	25.372	13.645	1.894	374	-	-5.059	.874
						.06	.13						1.697		
P6	.00146	.756	.248	.073	02	-	-	.534	24.756	9.554	2.104	584	-	-4.533	.860
						.07	.12						2.068		
P7	.00407	.767	.172	.067	.056	-	-	1.538	25.314	6.666	1.941	1.666	-	-5.879	.862
						.08	.16						2.403		
P8	.00459	.774	.132	.031	.037	-	-	1.784	25.606	5.122	.893	1.096	-	-6.015	.863
						.10	.16						2.926		
P9	.00086	.860	.066	.010	00	-	-	.402	30.766	2.784	.326	044	-	-5.427	.883
						.03	.13						1.052		
P10	.00160	.949	.002	01	01	.00	-	1.234	50.490	.136	569	446	.356	-5.143	.947
							.08								

Table 30: Profitability-Sorted Portfolios

<u>P</u>	<u>A</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj. R ²
P1	.00164	.662	.325	.043	029	221	09	.655	28.071	16.213	1.583	-1.09	-8.127	-4.230	.917
P2	.00424	.672	.313	.068	031	153	13	1.564	24.766	13.516	2.182	-1.05	-4.885	-5.627	.890
P3	.00503	.682	.313	.056	.071	230	07	2.122	28.954	15.634	2.076	2.746	-8.489	-3.423	.917
P4	.00123	.721	.319	.084	049	085	12	.486	26.286	13.650	2.666	-1.63	-2.702	-4.903	.887
P5	.00263	.731	.298	.092	.005	085	12	1.020	25.428	12.156	2.787	.166	-2.558	-4.767	.876
P6	.00240	.723	.299	.096	022	039	16	.881	22.925	11.126	2.652	624	-1.086	-5.746	.851
P7	.00141	.810	.267	.149	.021	.023	10	.631	28.600	11.061	4.614	.661	.693	-4.267	.880
P8	.00139	.865	.281	.108	005	.107	13	.653	31.309	11.934	3.412	151	3.36	-5.210	.886
P9	.00350	.892	.284	.078	.027	.125	11	1.716	32.708	12.237	2.494	.903	3.971	-4.778	.889
P10	.00558	.899	.294	03	.016	.127	12	2.367	30.179	11.601	-1.02	.475	3.708	-4.670	.867

Table 31: Value-Sorted Portfolios

<u>P</u>	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τ α</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	<u>Adj.</u>
															<u>R</u> ²
P1	.00320	.607	.466	.173	03	11	0	1.310	27.88	25.15	6.961	-1.51	-4.6	-3.06	.929
P2	.00120	.667	.388	.205	01	06	1	.503	27.88	19.04	7.514	571	-2.3	-4.81	.914
P3	0000	.727	.382	.190	.001	01	1	028	30.31	18.721	6.917	.040	56	-4.55	.914
P4	.00405	.685	.354	.102	00	09	1	1.673	26.14	15.852	3.396	286	-3.1	-6.31	.897
P5	.00310	.764	.288	.070	03	05	1	1.242	26.93	11.921	2.149	947	-1.7	-4.73	.880
P6	.00405	.775	.285	.069	.008	03	1	1.594	27.06	11.688	2.116	.242	91	-5.70	.877
P7	.00081	.798	.214	.049	.014	05	1	.330	27.50	8.679	1.488	.434	-1.5	-5.35	.874
P8	.00313	.783	.235	07	.039	09	2	1.342	27.87	9.823	-2.23	1.258	-2.8	-6.79	.882
P9	.00286	.826	.164	11	01	08	1	1.222	28.31	6.561	-3.44	488	-2.3	-5.54	.871
P10	.00077	.879	.147	15	.012	10	0	.385	32.81	6.444	-4.99	.394	-3.4	817	.893

Table 32: Momentum-Sorted Portfolios

<u>P</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj.
															<u>R</u> ²
P1	.0037	.521	.292	04	.020	23	32	.971	15.877	10.443	-1.07	.546	-5.98	-11.16	.839
P2	0002	.520	.240	.186	.063	21	13	05	12.203	6.614	3.814	1.348	-4.37	-3.383	.728
Р3	0006	.606	.252	.247	.034	12	02	18	14.127	6.899	5.033	.725	-2.50	611	.724
P4	.00249	.609	.252	.175	.018	18	.009	.703	14.065	6.826	3.543	.378	-3.54	.222	.719
P5	.00288	.638	.252	.167	00	20	13	.850	15.178	7.048	3.482	035	-4.24	3.466	.735
P6	.00166	.643	.252	.235	.065	17	.172	.489	14.640	6.745	4.674	1.332	-3.46	4.432	.711
P7	.00051	.670	.264	.211	01	13	.229	.149	15.066	6.956	4.141	233	-2.61	5.825	.703
P8	.00167	.695	.271	.138	.008	20	.368	.541	16.883	7.745	2.925	.175	-4.25	10.090	.746
P9	.00176	.685	.253	.138	.011	20	.436	.518	15.686	6.818	2.757	.227	-3.85	11.293	.714
P10	.00156	.660	.250	.034	.030	-	.596	.403	15.064	6.692	.673	.613	-	15.352	.712
						.216							4.274		

When the single-sorted portfolios are regressed against a six-factor model which consists of the five factors from the Fama-French Five-factor model plus an additional momentum factor, it is found that the model is able to explain a significant portion of the excess returns on almost all of the portfolios, with a few exceptions. The portfoliosP9 and P10, consisting of the most profitable companies, still manage to outperform the model at statistically significant levels of 10 percent and 5 percent confidence intervals respectively. Similarly, amongst portfolios formed on the basis of the Investment factor, the portfolio P10 also has a statistically significant Alpha-intercept. For portfolios formed on the basis of Size, the portfolio P1, consisting of the smallest companies by way of market cap, also outperforms the model at a statistically significant level. However, the Six-factor model does a great job of explaining the excess returns for all the portfolios formed on the basis of the Momentum factor, and all but one of the portfolios formed on the basis of the Value factor.

After regressing returns for single-sorted portfolios, the study then proceeds with testing the different asset-pricing models, those which are in contemporary use as well as those suggested by this study, against the mean-excess returns of double-sorted portfolios formed on the basis of the factors size-investment, size-value and size-profitability. The study then goes a step further and also tests the same models against portfolios formed on the basis of the size-momentum factors.

CAPM

Table 33: Size-Investment Sorted Portfolios

Portfolio	Alpha-	Beta Coefficient	<u>t-value</u>	T-value Beta	Adjusted R
	<u>intercept</u>		<u>Alpha</u>		<u>squared</u>
S/C	.0087	.767	1.865	18.440	.587
S/M	.0098	.805	2.457	20.898	.646
S/A	.0126	.820	3.126	22.069	.670
B/C	.0022	.879	.737	28.445	.772
B/M	.0026	.911	1.170	34.052	.829
B/A	.0027	.933	1.253	39.932	.870

Table 34: Size-Profitability Sorted Portfolios

Portfolio	Alpha-	Beta Coefficient	T-value	T-value Beta	Adjusted R
	<u>intercept</u>		<u>Alpha</u>		<u>squared</u>
S/W	.0070	.803	1.560	20.786	.643
S/M	.0010	.783	2.422	19.433	.612
S/R	.0168	.799	4.262	20.480	.636
B/W	.0018	.904	.614	32.562	.816
B/M	.0010	.906	.431	33.083	.821
B/R	.0042	.933	2.302	39.862	.869

Table 35: Size-Value Sorted Portfolios

Portfolio	Alpha-	Beta Coefficient	<u>T-value</u>	<u>T-value</u>	Adjusted R
	<u>intercept</u>		Aplha		<u>squared</u>
S/L	.0049	.814	1.191	21.625	.661
S/M	.0080	.812	2.066	21.474	.658
S/H	.0136	.765	2.863	18.321	.583
B/L	.0002	.938	.121	41.755	.879
B/M	.0038	.896	1.399	31.060	.801
В/Н	.0078	.826	1.933	22.567	.680

Table 36: Size-Momentum Sorted Portfolios

Portfolio	<u>Alpha-</u>	<u>Beta</u>	T-value	T-value	Adjusted R
	<u>intercept</u>	Coefficient	<u>Aplha</u>		<u>squared</u>
S/L	0004	.770	104	18.633	.592
S/W	.0198	.637	3.859	12.754	.403
B/L	.0019	.747	.430	17.321	.556
B/W	.0081	.693	2.172	14.840	.478

Regressing double-sorted portfolios against the single-index CAPM yields results that presents the model in a much better light when compared to the results of regressing the single-sorted portfolios against the same. For the portfolios sorted on the size-investment factors, the portfolios S/C (small size companies with a conservative approach towards investment), S/M (small size companies with a moderate growth in assets) and S/A (small size companies with an aggressive approach towards investment) show statistically significant Alpha-intercept at 10 percent confidence-interval for the first and at 5 percent confidence-interval for the latter two portfolios. For portfolios sorted on the basis of size and profitability factors, the portfolios S/M (small size companies with moderate profitability), S/R (small size companies with robust profit margins) and B/R (big companies with robust profits) outperform the model at statistically significant levels. When portfolios are sorted for size and value factors, it is found that small sized portfolios having moderate value and high value, namely S/M and S/H, show a statistically-significant Alpha-intercept at the 5 percent confidence interval while the portfolio B/H, comprising of big-sized companies having high value, also show a statistically significant Alpha-intercept, albeit at the 10 percent confidence interval. The study also finds that for portfolios sorted on size and momentum factors, the portfolios for the winners of both small cap companies and large cap companies, S/W and B/W outperform the single-factor CAPM at statistically significant levels as well. Additionally, when mean-excess returns of the

size-momentum portfolios are regressed against the CAPM, the single-index model also shows a comparatively lower value of the adjusted R squared. This would imply that even though the CAPM does a good job in explaining the returns of the double-sorted portfolios formed on all the other factors, it falls short when used to elucidate upon the returns of the portfolios formed on size and momentum.

Fama-French Three-Factor model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_t + \varepsilon_{it}$$

Table 37: Size-Investment Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	T-value1	T-value2	T-value3	Adjusted
					<u>value</u>				<u>R</u> ²
S/C	0053	.711	.481	.208	-2.556	38.658	25.085	10.741	.921
S/M	0013	.761	.453	.046	641	37.713	21.564	6.277	.905
S/A	.0024	.785	.425	.078	.977	34.157	17.742	3.250	.876
B/C	0037	.841	.125	.225	-1.494	33.608	4.800	8.540	.853
B/M	0010	.885	.101	.151	530	37.542	4.107	6.098	.870
B/A	.0008	.930	.144	043	.412	42.457	6.290	-1.867	.887

Table 38: Size-Profitability Sorted Portfolios

Portfolio	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-value1</u>	T-value2	T-value3	Adjusted
					<u>Value</u>				<u>R</u> ²
S/W	0060	.756	.463	.148	-2.765	41.001	24.057	7.660	.920
S/M	0019	.733	.460	.177	897	35.975	21.649	8.267	.903

S/R	.0065	.760	.445	.101	2.744	32.441	18.251	4.126	.871
B/W	0034	.874	.114	.170	-1.353	36.855	4.616	6.821	.868
B/M	0031	.880	.112	.150	-1.402	36.594	4.491	5.933	.864
B/R	.0025	.929	.146	033	1.423	42.462	6.419	-1.426	.888

Table 39: Size-Value Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-</u>	<u>T-</u>	T-value3	Adjusted R ²
					<u>Value</u>	<u>value1</u>	<u>value2</u>		
S/L	0017	.808	.445	143	598	30.905	16.332	-5.201	.840
S/M	0022	.773	.440	.103	-1.009	35.593	19.459	4.517	.889
S/H	0012	.705	.474	.245	641	43.182	27.893	14.278	.938
B/L	0009	.941	.149	083	566	45.604	6.953	-3.842	.900
B/M	0010	.864	.108	.187	436	35.167	4.206	7.246	.858
В/Н	0008	.768	.069	.396	303	30.866	2.667	15.152	.855

Table 40: Size-Momentum Sorted Portfolios

<u>Portfolio</u>	<u>Alpha</u>	Beta1	Beta2	Beta3	<u>T-</u>	<u>T-</u>	<u>T-</u>	T-value3	<u>Adjusted</u>
					Value	value1	<u>value2</u>		<u>R</u> ²
S/L	0013	.720	.406	.196	-4.308	27.742	15.017	7.184	.842
S/W	.0094	.597	.441	.108	2.287	15.158	10.744	2.619	.636
B/L	0035	.711	.089	.223	860	17.711	2.116	5.291	.622
B/W	.0060	.685	.141	.000	1.586	14.752	2.908	.008	.494

Thereafter, the double-sorted portfolios are then regressed against the Fama-French Three-Factor model. In comparison to the CAPM, the Three-Factor model does a better job at explaining the excess returns of the double-sorted portfolios. The model is able to explain the mean-excess returns for all but two of the double-sorted portfolios. Only the portfolios S/R, comprising of small cap stocks having high profitability, and S/W, which consists of small cap stocks having strong momentum effects, display statistically significant Alpha-intercepts. The values of the adjusted R-squared are also much higher than those observed for the single-index CAPM, which suggests that the Fama-French Three-factor model is more adept at explaining the excess portfolio returns. So far, one of the common threads being observed is that most of the portfolios that have outperformed the models being tested generally comprise of small stock companies. Additionally, both the single-index model and the three-factor model do not sufficiently explain the mean excess returns of portfolios which consist of past winners.

Carhart Four-Factor model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_{it} + \beta_3 MOM_{it} + \varepsilon_{it}$$

Table 41: Size-Investment Sorted Portfolios

<u>Portfoli</u>	<u>Alph</u>	<u>Beta</u>	<u>Beta</u>	<u>Beta</u>	<u>Beta</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>Adjuste</u>
<u>o</u>	<u>a</u>	<u>1</u>	<u>2</u>	<u>3</u>	<u>4</u>	<u>Value</u>	<u>value</u>	<u>value</u>	<u>value</u>	<u>value</u>	dR ²
						<u>A</u>	1	<u>2</u>	<u>3</u>	<u>4</u>	

S/C	-	.682	.482	.182	101	-1.281	37.27	26.53	9.593	-5.333	.929
	.0026						1	8			
S/M	.0013	.729	.454	.105	107	.630	36.23	22.72	5.062	-5.131	.914
							0	5			
S/A	.0061	.743	.426	.042	141	2.526	33.04	19.07	1.813	-6.043	.892
							9	0			
B/C	-	.802	.126	.190	134	224	32.14	5.092	7.357	-5.198	.868
	.0005						0				
B/M	.0016	.846	.102	.117	133	.827	36.22	4.389	4.833	-5.485	.884
							0				
B/A	.0038	.891	.144	077	134	1.928	41.49	6.779	-3.477	-5.998	.902
							8				

<u>Table 42: Size-Profitability Sorted Portfolios</u>

<u>Portfolio</u>	Alpha	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>Value</u>	value1	value2	value3	value4	$\underline{\mathbf{R}^2}$
S/W	0027	.721	.463	.118	119	-	40.272	26.055	6.357	-6.400	.932
						1.295					
S/M	.0006	.703	.460	.151	101	.288	34.355	22.661	7.120	-4.782	.911

S/R	.0094	.725	.446	.071	119	4.007	30.869	19.148	2.918	-4.891	.883
B/W	0000	.835	.115	.135	134	011	35.538	4.931	5.570	-5.511	.883
B/M	.0004	.832	.114	.108	163	.220	35.972	4.947	4.508	-6.803	.886
B/R	.0043	.900	.147	058	098	2.493	40.584	6.677	-2.524	-4.262	.895

Table 43: Size-Value Sorted Portfolios

Portfolio	<u>Alpha</u>	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>Value</u>	value1	value2	value3	value4	$\underline{\mathbf{R}^2}$
S/L	.0027	.758	.446	187	171	1.00	29.923	17.748	-7.124	-6.509	.864
0.04	0000	705	4.4.1	070	120	405	24.200	20.702	2166	5.504	002
S/M	.0008	.735	.441	.070	128	.405	34.389	20.792	3.166	-5.784	.903

S/H	.0012	.679	.475	.222	088	.645	41.744	29.420	13.200	-5.192	.944
B/L	.0012	.908	.150	112	111	.730	44.197	7.366	-5.261	-5.231	.910
B/M	.0026	.817	.109	.146	161	1.176	34.337	4.605	5.913	-6.535	.880
B/H	.0035	.720	.070	.354	164	1.323	29.907	2.939	14.204	-6.565	.877

Table 44: Size-Momentum Sorted Portfolios

Portfolio	<u>Alpha</u>	Beta1	Beta2	Beta3	Beta4	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	<u>T-</u>	Adjusted
						<u>Value</u>	value1	value2	value3	value4	$\underline{\mathbf{R}^2}$
S/L	595	.645	.408	.130	257	-	29.288	18.675	5.697	-	.897
						2.347				11.274	

S/W	0007	.717	.439	.213	.408	209	22.032	13.574	6.328	12.089	.775
B/L	.0021	.643	.090	.163	233	.536	16.218	2.289	3.978	-5.682	.666
B/W	0030	.823	.138	.121	.469	979	21.118	3.562	2.996	11.599	.677

When the mean-excess returns for the double sorted portfolios are regressed against the Carhart Four-Factor model, which is simply the Fama-French Three-Factor model with an added Momentum factor, some interesting results come to the fore. First, the Four-Factor model is tested by regressing the returns for portfolios sorted on the basis of size and investment effects against it. It is found that the portfolios S/A and B/A, comprising of small size and big size companies aggressively investing in assets, have statistically significant Alpha-intercepts at 5 percent and 10 percent confidence intervals. Thereafter, returns for portfolios sorted on the basis of size and profitability factors are regressed against the Carhart Four-Factor model. It is similarly found that the portfolios S/R, consisting of small size companies with robust profitability, and B/R, consisting of big sized companies with robust profitability, outperform the model when viewed in terms of the statistically significant Alpha-intercepts that are observed. Portfolios formed on the basis of Size and Value factors do not outperform the model as these effects are already subsumed in the factors that comprise the model. Similarly, portfolios formed on the basis of size and momentum effects also do not display statistically significant Alpha-intercepts for reasons similar to those mentioned previously. Furthermore, it is even more interesting to note that when portfolios formed using the Size and Value effects are tested against the Carhart, the Beta Co-efficient for the size and value effects are high and strong in terms of their statistical significance. However, the Beta Co-efficient for the momentum factor is extremely feeble. This is especially true in case of the portfolio S/H, which consists of small-size, high-value companies. On the other hand, portfolios formed on the Size and Momentum effects have statistically significant Beta Co-efficients not just for the momentum factor, but also for the size and value factors as well. These observations would seem to suggest the presence of a reversal effect, as that would be an appropriate explanation for the aforementioned observations.

Fama-French Five-Factor Model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_t + \\ + \beta_4 CMA_t + \beta_5 RMW_t + \varepsilon_{it}$$

Table 45: Size-Investment Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
S/C	.0064	.682	.453	.083	129	106	.322	34.008	26.212	3.633	-	-4.591	.938
											5.799		
S/M	0002	.729	.447	.125	.026	060	094	29.390	20.953	4.456	.956	-2.118	.906

S/A	.00123	.707	.431	.166	.202	103	.493	27.481	19.473	5.672	7.075	-3.505	.899
B/C	.00109	.826	.099	.101	143	080	.432	28.277	3.936	3.059	-	-2.377	.869
											4.399		
B/M	.0003	.855	.092	.127	.003	064	.154	29.443	3.683	3.846	.078	-1.917	.871
B/A	.0005	.867	.146	.012	.143	090	.244	33.802	6.602	.415	5.030	-3.072	.899

Table 46: Size-Profitability Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
S/W	.0002	.663	.434	.069	.003	-	.098	33.691	25.633	3.105	.151	-8.932	.941
						.202							
S/M	00003	.707	.450	.145	-	-	011	28.261	20.874	5.106	446	-2.062	.904
					.012	.059							
S/R	.0028	.804	.465	.170	.038	.109	1.138	28.562	19.170	5.313	1.226	3.386	.878
B/W	.0031	.745	.082	.093	.047	-	1.315	29.462	3.744	3.250	1.684	-9.148	.902
						.265							
B/M	0009	.831	.100	.120	.016	-	415	28.363	3.969	3.615	.502	-2.944	.868
						.099							
B/R	.0004	.963	.160	.012	.020	.080	.262	36.073	6.952	.403	.675	2.615	.891

Table 47: Size-Value Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	Adj.
													$\underline{\mathbf{R}^2}$
S/L	.0031	.713	.422	196	.040	194	1.053	23.339	16.039	-5.638	1.170	-5.539	.857
S/M	0006	.753	.432	.075	-	048	282	28.092	18.730	2.467	450	-1.568	.890
					.013								
S/H	.0011	.665	.464	.218	.010	082	.552	33.748	27.320	9.724	.441	-3.645	.940
B/L	.0001	.909	.142	098	.018	064	.082	35.825	6.517	-3.386	.639	-2.203	.901
B/M	.0005	.821	.099	.171	.029	084	.231	27.243	3.807	5.010	.862	-2.440	.861
B/H	.0029	.686	.051	.362	.049	161	.998	23.269	2.027	10.817	1.499	-4.767	.867

Table 48: Size-Momentum Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
S/L	0078	.628	.382	.137	.028	191	-2.519	20.698	14.624	3.969	.819	-5.471	.859
S/W	.0127	.542	.424	.059	-	120	2.891	11.195	10.166	1.070	036	-2.161	.640
					.002								
B/L	.0020	.576	.060	.171	.086	267	.468	12.120	1.465	3.172	1.638	-4.892	.654
B/W	.0086	.655	.123	068	-	082	2.122	11.434	2.496	-	876	-1.254	.496
					.056					1.050			

Returns of the double-sorted portfolios are then regressed against the Fama-French Five-Factor model, which consists of Investment and Profitability factors in addition to the three factors from the earlier model proposed by Eugene Fama and Kenneth French. It is intriguing to note that despite the fact that the Five-Factor model consists of an Investment factor, the Size and Value effects still carry significant explanatory power when concerned with the excess returns of portfolios formed on the size-investment sorts. This is found to be especially true for all three small size portfolios S/C, S/M and S/A. The Investment factor only carries statistically significant explanatory power in case of the portfolios S/A and B/A, which comprise of companies that are investing aggressively in assets. A similar trend can be observed when the returns for portfolios formed on the Size-Profitability sorts are regressed against the Five-Factor model. The Size and Value effects display statistically significant power in explaining the excess returns of all the small size portfolios S/W, S/M and S/R. The Profitability effect only helps explain the returns of portfolios S/R and B/R, which consists of companies that have robust profitability. The Alpha-intercepts of portfolios formed on the Size-Investment, Size-Profitability and Size-Value sorts are statistically insignificant, implying that the Five-Factor model does a fair job of explaining the returns of the aforementioned double-sorted portfolios. However, for portfolios sorted on the Size-Momentum factors, the Alpha-intercepts for the portfolios S/W and B/W, consisting of small size winners and big size winners respectively, are statistically significant. Moreover, the T-values for the Beta Co-efficients related to the Market and Size effects, while still statistically significant, show a sharp drop in case of both the Winner portfolios. Additionally, the values of the adjusted R squared are also lower than those observed for the model when testing against the other double-sorted portfolios. These observations, when summed up, would seem to suggest that the Five-Factor model is not as robust when explaining the excess returns on portfolios having strong Momentum effects.

Modified Five-Factor Model

$$R_{pt} - R_{ft} = \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 CMA_t + \beta_4 RMW_t + \beta_5 MOM_{it} + \varepsilon_{it}$$

Table 49: Size-Investment Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τ α</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	Adj. R ²
S/C	.0045	.665	.460	172	097	107	2.505	34.547	28.203	-9.623	-4.476	-6.377	.945
S/M	.0046	.711	.458	039	060	117	2.134	28.878	21.963	-1.697	-2.170	-5.450	.909
S/A	.0077	.685	.445	.116	107	142	3.273	26.752	20.515	4.880	-3.705	-6.385	.902
B/C	.00551	.802	.108	195	064	147	2.381	28.604	4.536	-7.495	-2.036	-6.013	.882
B/M	.0046	.832	.103	063	056	143	2.285	29.399	4.286	-2.405	-1.766	-5.821	.880
B/A	.0023	.847	.148	.137	059	117	1.236	34.663	7.129	6.051	-2.167	-5.496	.911

Table 50: Size-Profitability Sorted Portfolios

<u>Portfolio</u>	<u>A</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u> <u>R²</u>
S/W	.0038	.646	.440	033	190	104	2.096	34.462	27.735	-1.873	-9.026	-6.381	.947

S/M	.0052	.690	.462	088	064	116	2.380	27.344	21.614	-3.745	-2.274	-5.290	.905
S/R	.0091	.780	.479	050	.109	155	3.869	28.066	20.338	-1.929	3.495	-6.425	.884
B/W	.0072	.727	.089	001	257	113	3.245	29.390	4.268	047	-9.277	-5.246	.908
B/M	.0038	.840	.110	046	082	167	1.789	28.991	4.702	-1.783	-2.646	-6.944	.885
B/R	.0019	.944	.161	.014	.109	108	1.147	36.661	7.402	.583	3.757	-4.843	.901

Table 51: Size-Value Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τ α</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
S/L	-	.689	.407	.142	-	116	009	21.690	15.157	4.813	-	-4.203	.849
	.00003				.107						3.009		
S/M	.0031	.731	.439	052	-	134	1.413	28.603	20.282	-2.20	-	-6.025	.902
					.029						1.019		
S/H	.0087	.650	.481	104	-	109	4.086	29.340	25.631	-	-	-5.649	.926
					.109					5.029	4.395		
B/L	0006	.891	.135	.069	-	088	374	35.049	6.288	2.925	417	-3.985	.903
					.012								
B/M	.0068	.794	.113	060	-	174	2.903	27.110	4.560	-	-	-6.849	.872
					.080					2.210	2.421		
B/H	.0155	.659	.081	139	-	195	4.926	19.685	2.840	-	-	-6.686	.832
					.202					4.478	5.378		

Table 52: Size-Momentum Sorted Portfolios

<u>Portfolio</u>	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>Adj.</u>
													<u>R</u> ²
S/L	.00015	.587	.394	043	-	252	.060	23.068	18.310	-	-	-11.40	.903
					.154					1.824	5.379		
S/W	.0079	.616	.426	034	-	.413	2.401	16.191	13.221	953	-	12.497	.783
					.257						6.026		

B/L	.0094	.540	.074	002	-	221	2.363	11.701	1.905	051	-	-5.513	.681
					.248						4.785		
B/W	.00166	.739	.115	021	-	.485	.538	16.336	2.997	510	-	12.333	.693
					.206						4.064		

In accordance with the argument of Fama and French (2015), that the addition of a profitability factor to the Three-Factor model renders the Value effect as obsolete, the study then evaluates the efficacy of a modified Five-Factor model that does away with the Value factor but adds a Momentum factor in its place. All the other factors which are part of the Fama-French Five-Factor model are still in place. The study finds statistically significant Alpha-intercepts for all but one of the portfolios sorted on the basis of the Size-Investment effects. Similarly, only the portfolio B/R, which comprises of Big sized companies with robust profits, does not have a statistically significant Alpha-intercept. For portfolios sorted on the Size and Value effects, the portfolios S/H, comprising of small-sized high-value companies, the portfolios B/M and B/H, comprising of big companies with moderate value and high value respectively, also outperform the model at a statistically significant level. Surprisingly, for a model that has the Momentum effect as one of its constituents, even the portfolios sorted on Size-Momentum factors display statistically significant Alpha-intercepts. The portfolio S/W, comprising of small-sized winners, shows statistically significant outperformance while at the same time having a Beta Co-efficient for the Momentum factor which also has a statistically significant value. Surprisingly, even the portfolio B/L, comprising of big-sized losers, also shows a statistically significant Alpha-intercept. The observations related to the testing of portfolios sorted on the basis of the Size-Momentum effects would suggest the presence of a momentum effect in security returns, while at the same time making a case for the Value effect as well.

Six-Factor model

$$\begin{split} R_{pt} - R_{ft} &= \alpha_{it} + \beta_1 (R_{mt} - R_{ft}) + \beta_2 SMB_t + \beta_3 HML_t + \beta_4 CMA_t + \beta_5 RMW_t + \\ \beta_6 MOM_{it} + \varepsilon_{it} \end{split}$$

Table 53: Size-Investment Sorted Portfolios

<u>P</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τα</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj. R ²
S/C	.0029	.665	.455	.059	14	-	-	1.516	35.028	28.142	2.701	-6.750	-3.811	-5.831	.946
						.083	.098								
S/M	.0019	.711	.450	.100	.014	-	-	.873	29.661	22.034	3.663	.512	-1.344	-4.794	.914
						.037	.102								
S/A	.0039	.686	.434	.136	.187	-	-	1.654	28.046	20.857	4.851	6.920	-2.687	-5.641	.910
						.076	.122								
B/C	.0038	.803	.102	.068	16	-	-	1.570	28.836	4.323	2.134	-5.204	-1.517	-5.542	.884
						.049	.137								
B/M	.0025	.833	.095	.095	01	-	-	1.219	29.914	4.023	2.987	445	-1.077	-5.242	.884
						.035	.129								
B/A	.0027	.847	.149	02	.128	-	-	1.367	34.612	7.145	615	4.755	-2.247	-5.505	.910
						.063	.119								

Table 54: Size-Profitability Sorted Portfolios

<u>P</u>	<u>a</u>	<u>β1</u>	<u>B2</u>	<u>B3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τ α</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj. R ²
S/W	.00253	.646	.437	.046	01	18	-	1.297	34.740	27.571	2.139	434	-8.379	-5.905	.948
							.097								
S/M	.00207	.691	.452	.121	02	04	-	.911	28.405	21.852	4.353	921	-1.318	-4.561	.911
							.098								
S/R	.00566	.781	.468	.137	.021	.140	-	2.341	29.216	20.566	4.471	.725	4.548	-5.708	.893
							.135								
B/W	.00541	.727	.084	.068	.034	24	-	2.304	29.714	4.036	2.433	1.273	-8.585	-4.742	.910
							.103								

B/N	.0019	.805	.104	.082	00	06	-	.855	29.371	4.461	2.622	104	-2.019	-6.404	.887
							.155								
B/F	.0022	.944	.163	01	.006	.105	-	1.248	36.598	7.403	507	.216	3.541	-4.843	.900
							.111								

Table 55: Size-Value Sorted Portfolio

<u>P</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τ α</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj. R ²
S/L	.0064	.687	.425	23	.021	-	-	2.290	23.778	17.296	-7.035	.654	-4.806	-5.872	.875
						.160	.15								
S/M	.0019	.731	.435	.044	03	-	-	.847	28.691	20.069	1.504	-	657	-5.645	.903
						.019	.13					1.045			
S/H	.0029	.652	.466	.198	.000	-	-	1.517	34.127	28.645	9.074	016	-2.926	-4.712	.945
						.064	.08								
B/L	.0019	.890	.145	12	.005	-	-	1.076	36.375	6.957	-4.417	.173	-1.417	-4.904	.910
						.040	.10								
B/M	.0035	.795	.103	.133	.009	-	-	1.490	28.050	4.258	4.120	.302	-1.509	-6.166	.880
						.049	.15								
B/H	.0062	.661	.055	.326	.031	-	-	2.248	23.730	2.326	10.242	.999	-3.989	-5.939	.884
						.128	.15								

Table 56: Size-Momentum Sorted Portfolio

<u>P</u>	<u>a</u>	<u>β1</u>	<u>β2</u>	<u>β3</u>	<u>β4</u>	<u>β5</u>	<u>β6</u>	<u>Τ α</u>	<u>T1</u>	<u>T2</u>	<u>T3</u>	<u>T4</u>	<u>T5</u>	<u>T6</u>	Adj. R ²
S/L	002	.587	.388	.078	-	-	24	828	23.398	18.173	2.708	094	-4.701	-10.833	.906
					.003	.136									
S/W	.0035	.617	.413	.166	.053	-	.438	1.050	16.716	13.140	3.942	1.301	-5.163	13.394	.796
						.219									
B/L	.0062	.541	.065	.121	.061	-	20	1.497	11.827	1.670	2.316	1.207	-4.184	-5.022	.687
						.220									
B/W	.0005	.740	.111	.053	.006	-	.493	.175	16.345	2.875	1.019	.121	-3.730	12.302	.693
						.194									

The double-sorted portfolios are then regressed against a six-factor model that also incorporates a Momentum factor in addition to the five factors as proposed by Fama-French. Among the portfolios sorted on the basis of size-investment effects, only the portfolio S/A, consisting of small-sized companies which are aggressively investing in assets, shows a statistically significant Alpha-intercept at the 10 percent confidence interval. The Market and Size factors have a statistically significant impact on the mean-excess returns of the size-investment sorted portfolios. The Value effect also has a significant impact, from a statistical standpoint, on the returns of all of the size-investment portfolios except for the portfolio B/A, consisting big-sized companies which are aggressively investing in assets. For portfolios sorted on the basis of the Size and Profitability effects, the portfolios S/R, consisting of small-sized companies with robust profits, and, somewhat surprisingly, B/W, comprising of big-sized companies with weak profits, show statistically significant Alpha-intercepts. In case of portfolios sorted on the basis of Size and Value effects, only the portfolios S/L and B/H, small-sized low-value companies and big-sized high-value companies respectively, show statistically significant Alphaintercepts. The addition of a momentum effect to the Fama-French five factors seems to have subsumed the excess returns of the portfolios sorted on the Size-Momentum effects, which was evident in the earlier tests. The sum total of all these observations would indicate that momentum has to be taken into consideration when explaining portfolio returns.